

# D CUBE AURA

## CLASS XII – MATHEMATICS – CHAPTER 07

### INTEGRALS

Name:

Date:

**Q01.**  $\int \frac{x^3 - 1}{x^2} dx$

**Q03.**  $\int \frac{x^3 - x^3 + x - 1}{x - 1} dx$

**Q05.**  $\int_{-1}^2 |x^3 - 1| dx$

**Q07.**  $\int \frac{\sin^8 x - \cos^8 x}{1 - 2\sin^2 x \cdot \cos^2 x} dx$

**Q09.**  $\int (\sqrt{\cot x} + \sqrt{\tan x}) dx$

**Q11.**  $\int f'(ax + b)[f(ax + b)]^x dx$

**Q13.**  $\int_{-1}^1 \sin^5 x \cdot \cos^4 x dx$

**Q15.**  $\int_0^\pi \frac{x \sin x}{1 + \cos^2 x} dx$

**Q17.**  $\int \frac{5x}{(x+1)(x^2+9)} dx$

**Q19.**  $\int \left[ \log(\log x) + \frac{1}{(\log x)^2} \right] dx$

**Q21.**  $\int \frac{\cos 2x + 2\sin^2 x}{\cos^2 x} dx$

**Q23.**  $\int \frac{e^{5 \log x} - e^{4 \log x}}{e^{3 \log x} - e^{2 \log x}} dx$

**Q25.**  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{dx}{1 + \sqrt{\tan x}}$

**Q02.**  $\int \frac{\sec^2 x}{\cosec^2 x} dx$

**Q04.**  $\int \frac{\tan^4 \sqrt{x} \sec^2 \sqrt{x}}{\sqrt{x}} dx$

**Q06.**  $\int_0^\pi \frac{x \tan x}{\sec x + \tan x} dx$

**Q08.**  $\int \frac{dx}{\sqrt{\sin^3 x \sin(x+a)}}$

**Q10.**  $\int \cos^3 x \cdot e^{\log \sin x} dx$

**Q12.**  $\int_0^1 x e^x dx$

**Q14.**  $\int \frac{dx}{x+x \log x}$

**Q16.**  $\int_0^{\frac{\pi}{4}} \frac{\sin x + \cos x}{9 + 16 \sin 2x} dx$

**Q18.**  $\int \frac{\sin^{-1} \sqrt{x} - \cos^{-1} \sqrt{x}}{\sin^{-1} \sqrt{x} + \cos^{-1} \sqrt{x}} dx$

**Q20.**  $\int \frac{10x^9 + 10^x \log_e 10}{x^{10} + 10^x} dx$

**Q22.**  $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \sin^2 x dx$

**Q24.**  $\int \frac{e^{2x} - 1}{e^{2x} + 1} dx$

**Q26.**  $\int_0^{\frac{\pi}{4}} \frac{\sin x \cdot \cos x}{\cos^4 x + \sin^4 x} dx$

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**Q27.**  $\int \frac{dx}{\cos(x+a) \cdot \cos(x+b)} dx$

**Q29.**  $\int_0^{\frac{\pi}{2}} \log \sin x dx$

**Q31.**  $\int \frac{(x+1)(x+\log x)^2}{x} dx$

**Q33.**  $\int \frac{dx}{x^2 - 16}$

**Q35.**  $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) dx$

**Q37.**  $\int_1^4 [|x-1| + |x-2| + |x-3|] dx$

**Q39.**  $\int_0^1 \tan^{-1} \frac{2x-1}{1+x-x^2} dx$

**Q41.**  $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} (x^3 + x \cos x + \tan^5 x + 1) dx$

**Q43.**  $\int \frac{2+\sin 2x}{1+\cos x} e^x dx$

**Q45.**  $\int_{-1}^{\frac{3}{2}} x \sin(\pi x) dx$

**Q47.** Prove  $\int \sec x dx = \log |\sec x + \tan x| + c.$

**Q48.** Find sum of limit  $\int_0^4 (x + e^{2x}) dx.$

**Q49.** If  $f(a+b-x) = f(x)$  then  $\int_a^b f(x) dx = ?$

**Q50.** Show that  $\int_0^a f(x) \cdot g(x) dx = 2 \int_0^a f(x) dx.$  If  $f(x) = f(a-x)$  and  $g(x) + g(a-x) = 4.$

**Q28.**  $\int_0^{\frac{\pi}{2}} \frac{\cos^2 x}{\cos^2 x + 4 \sin^2 x} dx$

**Q30.**  $\int \frac{\sqrt{\tan x}}{\sin x \cdot \cos x} dx$

**Q32.**  $\int \frac{\cos 2x - \cos 2\alpha}{\cos x - \cos \alpha} dx$

**Q34.**  $\int e^x \left( \tan^{-1} x + \frac{1}{1+x^2} \right) dx$

**Q36.**  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sin x + \cos x}{\sqrt{\sin 2x}} dx$

**Q38.**  $\int_0^{\pi} \frac{x dx}{a^2 \cos^2 x + b^2 \sin^2 x}$

**Q40.**  $\int_0^{\frac{\pi}{2}} \left( \frac{4+3 \sin x}{4+3 \cos x} \right) dx$

**Q42.**  $\int_0^{\frac{\pi}{2}} (2 \log \sin x - \log \sin 2x) dx$

**Q44.**  $\int \tan^{-1} \sqrt{\frac{1-x}{1+x}} dx$

**Q46.**  $\int \frac{dx}{3x^2 + 13x - 10}$